

Figure 2. The Mathieu stability diagram in two dimensions (x and y). Regions of simultaneous overlap are labeled A , B , C , and D . [1]

suitable substitutions for the Mathieu parameters a and q to convert the axes into RF-DC voltage space for m/z 219, with r_0 calculated based on a 9.5 mm round quadrupole rod diameter, and an operating frequency Ω of 1.2 MHz.

For any set of RF and DC voltages, one could read directly from this figure whether ions of m/z 219 would have stable trajectories through a 9.5 mm quadrupole operated at 1.2 MHz. The area inside the boundaries represent voltages with stable trajectories, and the area outside the boundaries represent unstable trajectories for that stability region.

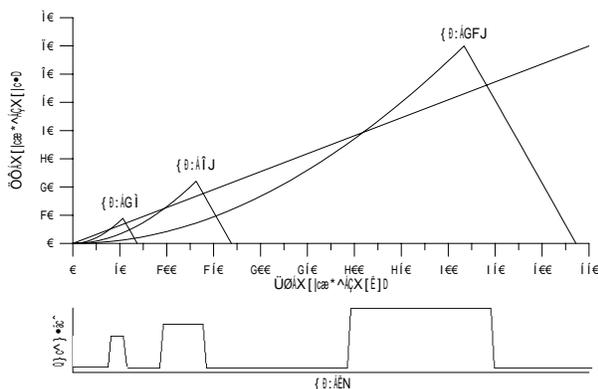


Figure 4. Stability diagrams for m/z 28, 69 and 219 plotted in RF-DC space, showing a straight scan line through the origin. The lower portion of the figure represents the mass peak widths resulting from the scan line passing into and out of the stability regions for each of the masses.

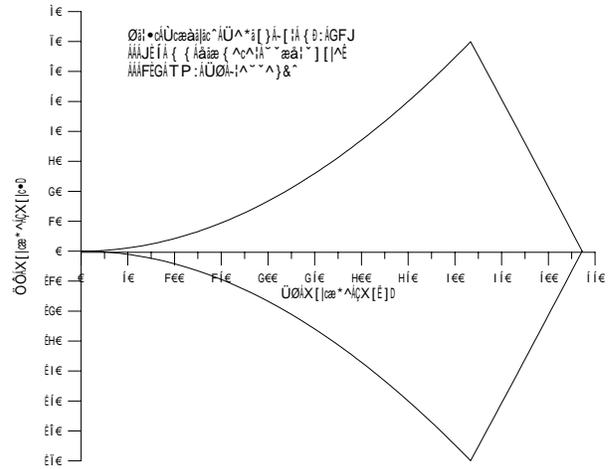


Figure 3. Expanded view of region A from Figure 2 (the ‘First Stability Region’) with suitable substitutions for a and q to convert into RF and DC space for mass 219 for a 9.5 mm quadrupole operated at 1.2 MHz.

IV. CONSTANT RESOLUTION SCANS

Note that the stability diagram shown in Figure 3 is symmetric around the DC voltage = 0 axis. In practice, when one assigns positive DC voltages to one rod pair, and negative DC voltages to the other pair, only the top half of this diagram is considered, with the bottom half of the diagram accessible by simply swapping the electrical connections to the quadrupole.

Figure 4 represents the stability diagrams for multiple masses plotted in the same RF-DC space. A linear scan line is drawn from the origin through the stability regions, passing from instability to stability back to instability for each of the masses. The bottom portion of Figure 4 represents the ion current that would be measured if RF and DC voltages are scanned through the values along this scan line as a function of time. If ions of various masses are directed into the quadrupole entrance, only certain ions will pass through the quadrupole to a detector at the exit, depending on whether the voltages yield stable trajectories. The various mass peak widths and positions correlate to the boundaries of their associated stability diagrams.

With a linear scan line through the origin, peak widths increase geometrically with increasing mass! (constant resolution)

If the slope of the mass scan line is decreased (dotted scan line in Figure 5), the scan line passes through a wider portion of the stability diagram, effectively widening the mass peak.

Note that the leading edge of the stability diagram comes up three times more slowly than the trailing edge goes down. The net result of this characteristic shape

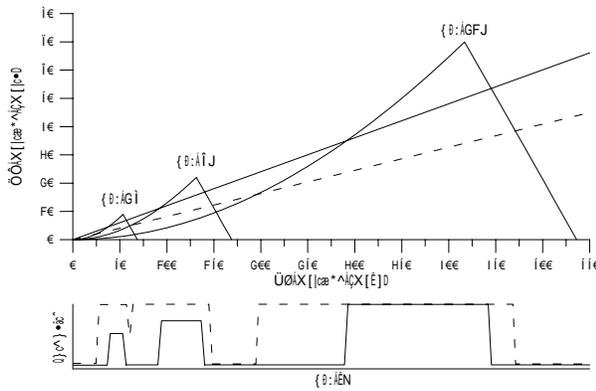


Figure 5. When the slope of the scan line is reduced (dotted scan line through the stability diagrams), the mass peaks widen, with the center of mass position moving to lower apparent mass.

of the stability diagram is that as the resolution is decreased (making the peak wider) the location of the leading edge of the mass peak moves to lower apparent mass three times faster than the trailing edge of the mass peak moves to higher apparent mass, yielding a shift of the center of the mass peak to lower apparent mass.

Changes to Mass Resolution result in predictable changes in Mass Calibration!

V. UNIT MASS RESOLUTION SCANS

Traditional treatments of quadrupole theory, including references 1 and 2 generally suggest that the typical quadrupole scan line is one with a constant *a/q* ratio (i.e. scan line drawn through the origin with constant slope in RF-DC space yielding constant mass

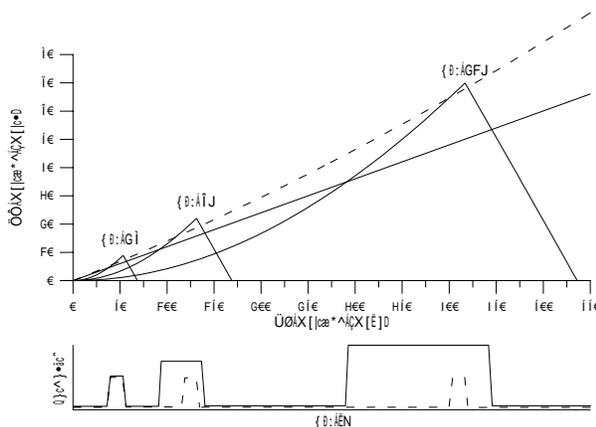


Figure 7. In order to achieve constant peak width across the mass range, a scan line that goes through the origin must be a curve with an increase in the DC to RF voltage ratio with increasing mass (dotted line in figure above).

resolution).

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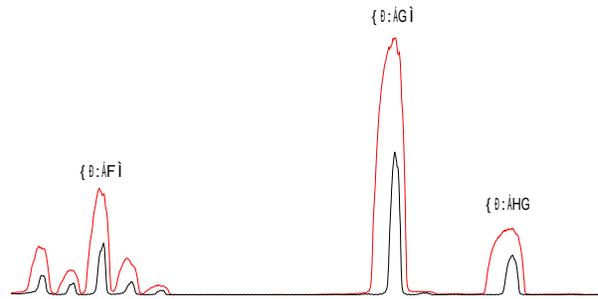


Figure 6. Experimental mass scan from m/z 15 to 35 demonstrating two different mass resolutions. Note that the scan showing wider peaks (red line) demonstrate lower apparent mass positions than the narrower mass peaks, as predicted by theory. These spectra were acquired using the Extrel Merlin Automation data system, and were gathered using a 19 mm tri-filter quadrupole operated at 1.2 MHz.

Commercial quadrupoles are almost **never** operated in this constant resolution mode, rather they are generally operated with a mass resolution that increases linearly with increasing mass (i.e. constant peak width, or Unit Mass Resolution).

To achieve unit mass resolution across the mass range, a scan line that goes through the origin must be a curve with an increase in the DC to RF voltage ratio with increasing mass. (See Figure 7.)

Historically, this curved ideal scan line has been approximated using a straight line in analog hardware by raising the slope of the scan line and lowering its intercept so as to not go through the origin. (See Figure 8). The intercept and slope are generally set empirically by simultaneously optimizing light and heavy calibration masses to unit mass resolution. Unfortunately, masses between these endpoint masses will not have constant peak width using a straight scan line.

In Extrel systems, the intercept, which primarily affects low mass resolution, is called delta-M, and the slope of the scan line, which primarily effects high mass resolution, is called delta-Res. This nomenclature is rumored to be taken from a paper or report published in the early 1960's by someone at MIT???

The 'error function' that represents the difference between the straight line approximation and the 'ideal' curved scan function (see Figure 9) has been implemented in commercial systems both in analog electronic circuitry and in software.

Extrel traditionally calls such an analog correction circuit the 'linearizer' circuit. Other manufacturers are rumored to have similar circuits in their designs.

VI. CONCLUSIONS

The purpose of this presentation is to de-mystify the theory associated with how quadrupoles operate.

